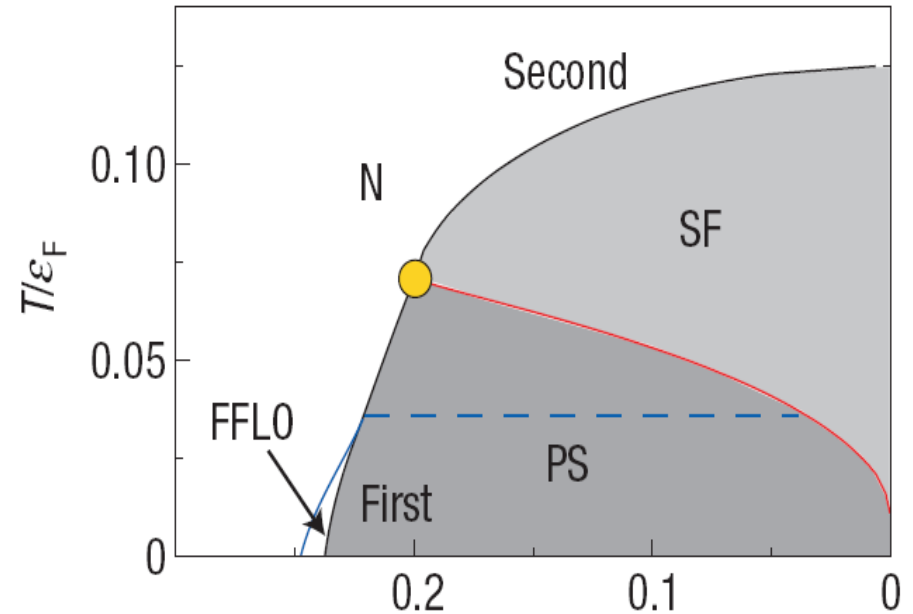


Cooling across a superfluid-normal interface in spin-imbalanced fermions - An analogue of a dilution fridge ?

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Spin-imbalanced fermions close to unitarity

- The phase diagram of spin-imbalanced fermionic atoms interacting via a feshbach resonance shares interesting features with $\text{He}_3\text{-He}_4$ mixture.
- At higher temperatures there is a line of second order transitions between a paired superfluid and normal leading to a tri-critical point.
- Below the tri-critical point the transition turns first order and the system phase separates between partially polarized normal and an unpolarized superfluid.



$$n/2 \equiv (n_{\uparrow} + n_{\downarrow})/2$$

$$m \equiv n_{\uparrow} - n_{\downarrow}$$

Mean-field phase diagram at $1/k_F a = -1$
 Parish et. al., Nature Physics 3, 124 - 128 (2007)

Only qualitatively correct (except perhaps FFLO) but quantitatively inaccurate.

Experiments with spin-imbalanced fermions (MIT)

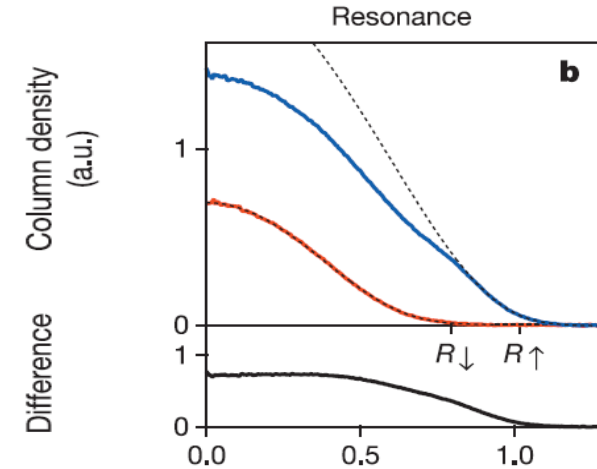
Zwierlein et. al., Nature (London) 442, 54 (2006)

- The polarized superfluid is unstable at high polarization. What is critical polarization at equilibrium ?

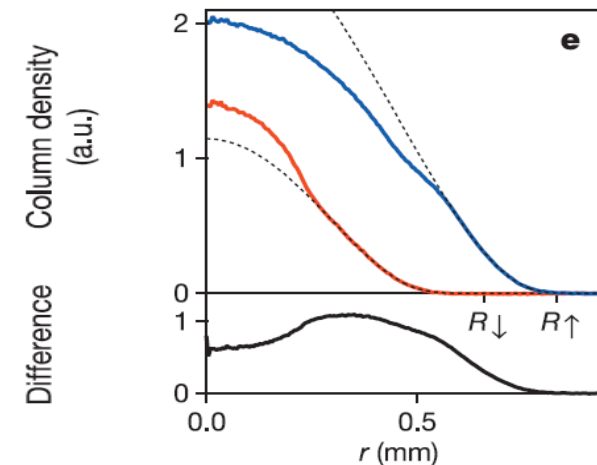
Polarization δ is defined to be

$$\delta = (N_{\uparrow} - N_{\downarrow}) / (N_{\uparrow} + N_{\downarrow})$$

- The critical polarization observed in the MIT group $\delta_c \approx 0.7$ (consistent with QMC predictions assuming Local Density approximation(LDA))
- Trap aspect ratio ≈ 5



Normal state
 $\delta = 0.63$
 $T/T_F = 0.15$

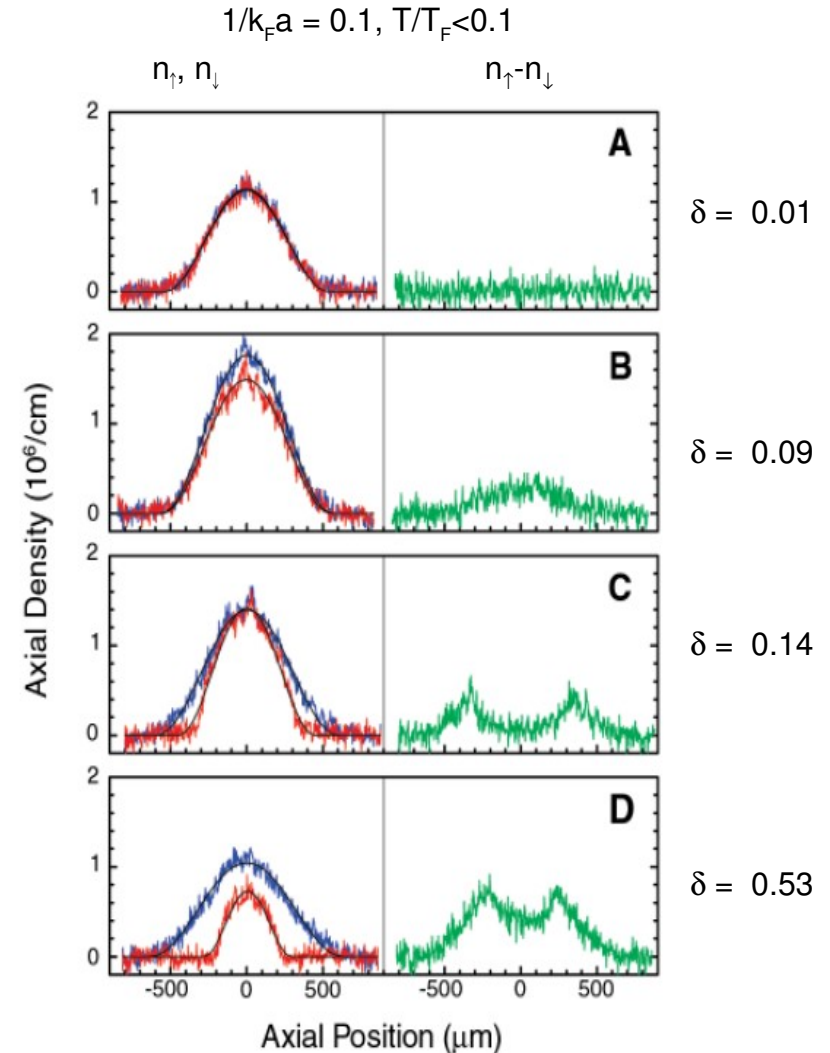


Superfluid state
 $\delta = 0.60$
 $T/T_F = 0.06$

Experiments with spin-imbalanced fermions (Rice)

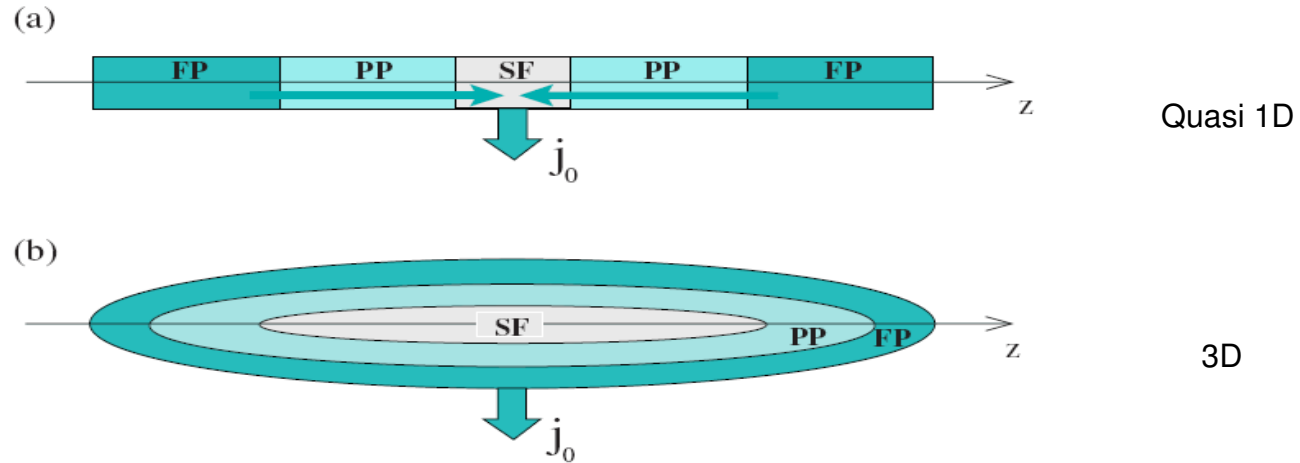
Partridge et. al., Science 311, 503 (2006)

- The critical polarization observed in the Rice group $\delta_c \approx 0.9$ (apparent violation of Clogston limit)
- Trap aspect ratio ≈ 30
- The spin densities violate LDA
- Both experiments report temperatures which are low enough for δ_c to be close to the $T=0$ value.



Non-equilibrium scenario in quasi 1D

Meera Parish and David Huse
Phys. Rev. A 80, 063605 (2009)



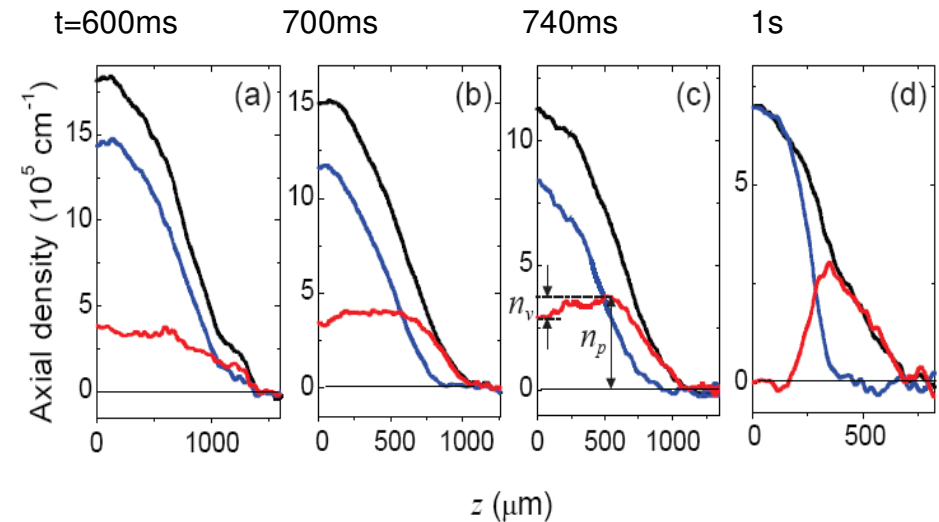
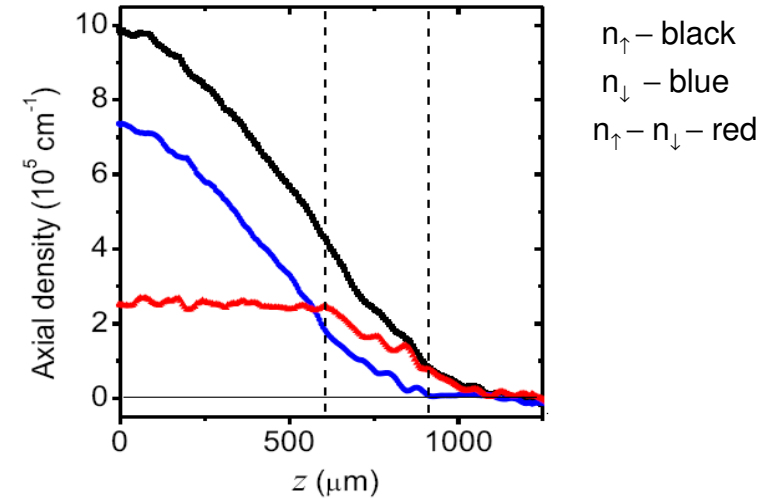
- For a highly elongated trap, evaporation occurs from the SF phase predominantly removing \uparrow atoms at low T .
- This generates a chemical potential gradient producing a spin current along the axial direction.
- But the spin-gap of the SF blocks spin current across the SF-N interface thus effectively depolarizing the SF.

Metastable phase

Y. A. Liao, et. al., arXiv:1105.6369

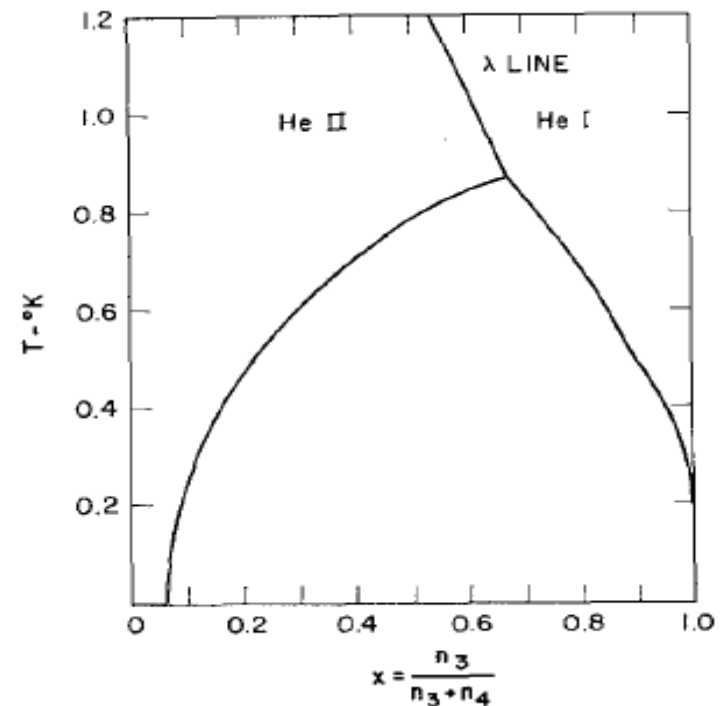
- Ramping the trap depth exponentially from $U=160\mu\text{K}$ to $2.2\mu\text{K}$ over 3.4s.
- Consistent with predictions based on LDA.
- Ramping the trap depth exponentially from $U=160\mu\text{K}$ to $0.74\mu\text{K}$ over 1s (more aggressive evaporation).
- A dip in the central density difference violating LDA.

$t=3.4\text{ s}; T/T_F=0.09$



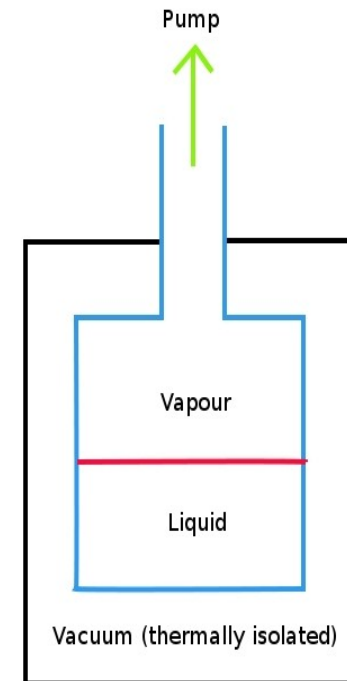
He₃ – He₄ mixture phase diagram

- At high temperatures, there is the λ -transition between superfluid and normal phase of He₄. Critical temperature is suppressed by the presence of fermionic He₃.
- At low temperatures, the system phase separates into a He₃ rich phase (“liquid”) and a dilute solution of He₃ in He₄ superfluid (“vapour”).
- Even at T=0 there is a finite concentration of He₃ in He₄ due to the degeneracy of the He₃ fermions and interaction effects.



Basic working-principle of a dilution fridge

- For the $\text{He}_3\text{-He}_4$ mixture, the “**vapour**” phase corresponds to the dilute solution of He_3 in superfluid He_4 which is effectively at $T=0$.
- The “**liquid**” phase corresponds to the concentrated He_3 with very little He_4 .
- Evaporating the He_3 atoms from the “**liquid**” phase results in cooling the “**liquid**” and the **interface** separating the 2 phases.



Transport across SF-N interface

- Under conditions when the system is driven (via evaporative cooling) a steady state can be established where

$$\mu_{\uparrow}^N + \mu_{\downarrow}^N \neq 2\mu_{SF}$$

due the blockage of spin transport across the interface.

- Another consequence of such a mechanism, would inhibit the transmission of heat thus resulting in a gradient in temperature as well.

$$T_N \neq T_{SF}$$

